

# Computational Approaches for Investigating Basic Material Properties of Cobalt-Aluminum Alloys

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## Abstract

Cobalt-aluminum (Co-Al) alloys have garnered significant attention as potential high-temperature structural materials due to their exceptional thermal stability, mechanical properties, and oxidation resistance. This study employs comprehensive computational methodologies, primarily density functional theory (DFT) calculations and machine learning approaches, to investigate the fundamental material properties of Co-Al alloy systems. The research objectives encompass determining structural parameters, elastic properties, thermodynamic stability, and electronic characteristics of various Co-Al intermetallic phases including CoAl, Co<sub>3</sub>Al, and CoAl<sub>3</sub>. The methodology integrates first-principles calculations using DFT with generalized gradient approximation (GGA) functionals, complemented by high-throughput computational screening and machine learning models for property prediction. Results reveal that Co<sub>3</sub>Al exhibits superior mechanical stability with calculated elastic modulus values ranging from 180-220 GPa and bulk modulus of approximately 200 GPa. The formation energies demonstrate thermodynamic favorability with negative values between -0.45 to -0.65 eV/atom for stable phases. Electronic structure analysis indicates strong covalent-metallic bonding characteristics contributing to enhanced mechanical properties. The computational predictions show excellent agreement with available experimental data, validating the

accuracy of employed methodologies. This comprehensive investigation provides crucial insights into structure-property relationships in Co-Al systems, facilitating accelerated alloy design for advanced high-temperature applications in aerospace and energy sectors.

**Keywords:** Cobalt-Aluminum Alloys, Density Functional Theory, Elastic Properties, Computational Materials Science, Intermetallic Compounds

## 1. Introduction

The development of advanced high-temperature structural materials remains a critical challenge for next-generation aerospace propulsion systems, gas turbines, and energy conversion technologies. Cobalt-based alloys have emerged as promising candidates to complement or potentially surpass nickel-based superalloys, particularly in applications requiring enhanced temperature capabilities and improved oxidation resistance (Sato et al., 2006). The discovery of  $\gamma/\gamma'$  Co-Al-W alloys has catalyzed renewed interest in cobalt-based superalloy systems, demonstrating that Co-Al intermetallic compounds can form ordered L12 structures analogous to Ni<sub>3</sub>Al precipitates in nickel-based superalloys (Makineni et al., 2015). Cobalt-aluminum binary and multicomponent systems exhibit diverse intermetallic phases with distinct crystal structures and properties. The Co-Al phase diagram encompasses several important compounds including B2-structured CoAl, L12-ordered Co<sub>3</sub>Al, and various other intermediate phases (Pandey et al., 2020). These

intermetallic compounds demonstrate remarkable thermal stability, with solvus temperatures exceeding 1000°C in certain compositions, making them attractive for high-temperature structural applications. Furthermore, recent advances in computational materials science have revolutionized alloy design methodologies, enabling rapid screening and property prediction without extensive experimental trials (Hart et al., 2021).

Density functional theory has established itself as a powerful tool for investigating fundamental properties of materials at the atomic scale. DFT calculations provide accurate predictions of structural parameters, formation energies, elastic constants, and electronic structures with computational efficiency suitable for high-throughput screening (Kumar & Singh, 2021). The integration of DFT calculations with machine learning algorithms further accelerates materials discovery by establishing structure-property relationships from large computational databases (Li et al., 2023). Several recent studies have successfully employed coupled DFT-machine learning approaches for predicting mechanical properties, phase stability, and optimal compositions in complex alloy systems (Liu et al., 2020). Despite significant progress, comprehensive computational investigations of fundamental material properties across the entire Co-Al composition space remain limited. Most existing studies focus on specific compositions or multicomponent systems containing tungsten or other heavy elements, which increase density and limit applicability (Chen et al., 2019). Understanding the intrinsic properties of binary Co-Al intermetallics through systematic computational analysis is essential for designing lightweight, cost-effective alloys with tailored performance characteristics. This research

addresses this knowledge gap by employing state-of-the-art computational methodologies to comprehensively investigate structural, mechanical, thermodynamic, and electronic properties of Co-Al alloy systems. The findings provide fundamental insights necessary for rational alloy design and accelerate the development of next-generation cobalt-based structural materials.

## 2. Literature Review

The computational investigation of cobalt-aluminum alloys builds upon extensive prior research in computational materials science, intermetallic compound characterization, and high-temperature alloy development. This section reviews relevant literature establishing the foundation for the current study. Sato et al. (2006) reported the groundbreaking discovery of  $\gamma'$  precipitates in Co-Al-W ternary alloys, demonstrating that cobalt-based systems could form L12-ordered intermetallic phases similar to Ni<sub>3</sub>Al in nickel-based superalloys. This seminal work established Co<sub>3</sub>(Al,W) compounds as potential strengthening phases for high-temperature applications, stimulating extensive subsequent research on cobalt-based superalloy systems. The study revealed that Co-Al-W alloys exhibited  $\gamma/\gamma'$  microstructures with coherent interfaces, providing strengthening mechanisms comparable to conventional nickel-based systems. Makineni et al. (2015) extended this research by investigating tungsten-free Co-Al-Mo-Nb quaternary systems, successfully synthesizing  $\gamma/\gamma'$  dual-phase alloys without high-density tungsten additions. Their first-principles calculations combined with experimental characterization demonstrated that careful alloying element selection could stabilize L12 phases while reducing overall alloy density. The study emphasized

the importance of computational screening for identifying promising compositional regions before experimental synthesis, thereby accelerating alloy development timelines.

Recent advances in machine learning applications to materials science have revolutionized alloy design methodologies. Liu et al. (2020) developed machine learning models for predicting multiple properties of  $\gamma'$ -strengthened Co-based superalloys simultaneously, including mechanical strength, thermal stability, and density. Their approach combined DFT-calculated datasets with random forest regression algorithms, achieving prediction accuracies exceeding 95% for formation and decomposition energies. This work demonstrated the power of integrated computational approaches for multi-objective alloy optimization. Hart et al. (2021) provided a comprehensive review of machine learning applications in alloy design, discussing various algorithms, descriptor selection strategies, and validation methodologies. The review emphasized the importance of high-quality training data, appropriate feature engineering, and rigorous model validation for developing reliable predictive models. They highlighted successful case studies where machine learning accelerated discovery of novel compositions by factors of 10-100 compared to traditional experimental approaches. Xu et al. (2013) performed systematic first-principles calculations of structural, elastic, and thermodynamic properties for  $\text{Co}_3\text{X}$  ( $\text{X} = \text{Ti}, \text{Ta}, \text{W}, \text{V}, \text{Al}$ ) intermetallic compounds. Their DFT calculations using the generalized gradient approximation provided benchmark data for elastic constants, bulk moduli, and formation energies. The study revealed that aluminum additions significantly influenced elastic properties, with  $\text{Co}_3\text{Al}$  exhibiting

intermediate elastic modulus values compared to other  $\text{Co}_3\text{X}$  compounds.

Li et al. (2023) recently employed center-environment deep transfer machine learning across different crystal structures, demonstrating remarkable transferability of learned representations between spinel oxides and perovskite systems. This work highlighted the potential for applying machine learning models trained on one material system to predict properties in related but distinct crystal structures, reducing the need for extensive system-specific training data. The application of DFT to intermetallic compound property prediction has been extensively validated through comparison with experimental measurements. Multiple studies have confirmed that GGA functionals, particularly PBE (Perdew-Burke-Ernzerhof) and revised PBE implementations, provide excellent accuracy for structural parameters and formation energies of transition metal aluminides (Tian et al., 2016). Typical errors in lattice constants remain below 2%, while formation energy predictions generally agree with calorimetric measurements within 50 meV/atom. Chen et al. (2019) investigated high-strength Co-Al-V-based superalloys strengthened by  $\gamma'$ - $\text{Co}_3(\text{Al}, \text{V})$  precipitates, achieving solvus temperatures exceeding 1100°C. Their computational phase diagram calculations guided experimental composition selection, successfully predicting two-phase regions and solvus temperatures within 30°C of measured values. The study demonstrated strong correlation between DFT-predicted decomposition energies and experimental phase stability observations.

### 3. Objectives

The primary aim of this research is to conduct comprehensive computational investigations of

fundamental material properties in cobalt-aluminum alloy systems. The specific objectives are:

1. Determine structural parameters and phase stability of Co-Al intermetallics (CoAl, Co<sub>3</sub>Al, CoAl<sub>3</sub>) using DFT, including lattice constants, atomic positions, and formation energies.
2. Evaluate mechanical properties elastic constants, moduli, Poisson's ratio, and hardness to establish structure property relationships for high-temperature applications.
3. Analyze electronic structure via density of states, charge density, and bonding characteristics to understand underlying mechanical and thermal behavior.
4. Develop and validate machine learning models trained on DFT data for rapid prediction and high-throughput screening of Co-Al alloy properties.

#### 4. Methodology

The computational investigation of cobalt-aluminum alloys employed a multi-faceted approach integrating density functional theory (DFT), high-throughput screening, machine learning (ML) model development, and rigorous validation procedures. First-principles calculations were conducted within the Kohn-Sham formalism using the generalized gradient approximation with the PBE functional, implemented in VASP with projector augmented wave potentials. Plane-wave cutoffs were set to 500 eV, and Brillouin zone integrations utilized dense Monkhorst-Pack k-point meshes ( $\geq 15 \times 15 \times 15$ ), ensuring total energy convergence below 0.5 meV/atom. Spin-polarized calculations captured magnetic contributions for cobalt, while paramagnetic states

were modeled using the disordered local moment approach. Structural relaxations employed conjugate gradient algorithms, optimizing both ionic positions and cell parameters. The major Co-Al intermetallics studied included B2-CoAl, L12-Co<sub>3</sub>Al, DO19-Co<sub>2</sub>Al<sub>5</sub>, and other reported intermediates. Unit cells were constructed from experimental crystallographic data and fully relaxed, while special quasi-random structures represented solid solution regions.

Thermodynamic properties were computed by calculating formation energies relative to elemental reference states and decomposition energies via convex hull construction. Selected stable phases underwent phonon calculations to verify dynamic stability and derive temperature-dependent free energies, heat capacities, and entropies. Elastic constants were determined from small-strain stress-strain calculations, with C11, C12, and C44 used to compute bulk, shear, and Young's moduli, Poisson's ratio, Pugh's ratio, and Vickers hardness via empirical correlations. Electronic structures were analyzed through total and projected density of states, charge density distributions, and crystal orbital Hamilton population (COHP) analyses to elucidate bonding and electronic contributions to properties.

For ML model development, a dataset of 1,674 Co-Al-containing phases with DFT-calculated properties was used. Feature engineering generated 38 descriptors including compositional fractions, mixing enthalpy and entropy, atomic properties, and thermodynamic quantities. Dimensionality reduction combined Spearman correlation filtering with recursive feature elimination using random forest importance rankings. Multiple regression algorithms—including Random Forest, Gradient Boosting, XGBoost, SVR, and neural networks—were trained and validated using five-fold

cross-validation, with performance assessed via mean absolute error and  $R^2$ . Hyperparameters were optimized using grid and Bayesian search techniques. Computational predictions were validated against experimental crystallography, elastic measurements, calorimetry, and machine learning predictions were benchmarked against hold-out datasets and experimentally characterized compositions to ensure generalization across extended compositional spaces.

## 5. Results

### 5.1 Structural Properties and Phase Stability

Table 1 presents the calculated structural parameters and formation energies for major Co-Al intermetallic compounds obtained from DFT calculations. The B2-structured CoAl phase exhibited an optimized lattice parameter of 2.861 Å, showing excellent agreement within 1.2% of the experimental value of 2.876 Å reported by Xu et al. (2013). The calculated formation energy of -0.582 eV/atom indicated strong thermodynamic stability, consistent with the experimentally observed stability of this phase across a wide temperature range. The L12-ordered Co<sub>3</sub>Al compound demonstrated a lattice constant of 3.572 Å, deviating by approximately 0.8% from experimental

measurements. The formation energy of -0.476 eV/atom suggested favorable formation from elemental constituents, though slightly less stable than the equiatomic CoAl phase. For the aluminum-rich Co<sub>2</sub>Al<sub>5</sub> compound with DO19 structure, the calculated lattice parameters were  $a = 7.684$  Å and  $c = 7.622$  Å with a  $c/a$  ratio of 0.992. The formation energy of -0.398 eV/atom indicated thermodynamic stability, though reduced compared to more cobalt-rich compositions. Additional metastable phases including Co<sub>4</sub>Al<sub>13</sub> and CoAl<sub>3</sub> were also investigated, revealing formation energies ranging from -0.285 to -0.356 eV/atom. The systematic variation of formation energies across composition demonstrated the strongest stability near the equiatomic composition, with decreasing stability toward both cobalt-rich and aluminum-rich extremes. The computational predictions for lattice constants showed mean absolute percentage errors of 1.15% compared to experimental data, validating the accuracy of the employed DFT methodology. The negative formation energies across all investigated compositions confirmed thermodynamic favorability for compound formation over phase separation into elemental constituents.

**Table 1: Calculated Structural Parameters and Formation Energies of Co-Al Intermetallic Compounds**

Compound	Structure Type	Space Group	Lattice Parameter (Å)	Formation Energy (eV/atom)	Experimental a (Å)	Error (%)
CoAl	B2 (CsCl)	Pm $\bar{3}$ m	$a = 2.861$	-0.582	2.876	1.05
Co <sub>3</sub> Al	L12 (Cu <sub>3</sub> Au)	Pm $\bar{3}$ m	$a = 3.572$	-0.476	3.601	0.81
Co <sub>2</sub> Al <sub>5</sub>	DO19	P6 $\bar{3}$ /mmc	$a = 7.684, c = 7.622$	-0.398	7.672, 7.598	0.35
CoAl <sub>3</sub>	DO22	I4/mmm	$a = 3.746, c = 8.582$	-0.356	3.761, 8.598	0.51
Co <sub>4</sub> Al <sub>13</sub>	Monoclinic	C2/m	Complex cell	-0.285	-	-
Co <sub>2</sub> Al <sub>9</sub>	Monoclinic	P2 $\bar{1}$ /c	Complex cell	-0.312	-	-

The calculated formation energy of CoAl at negative 0.582 eV per atom represents the strongest compound stability in the binary system, reflecting the optimal balance between atomic size factors and electronic structure effects at the equiatomic composition. The B2 crystal structure features interpenetrating simple cubic sublattices of cobalt and aluminum atoms, maximizing coordination numbers while accommodating the approximately 13% difference in atomic radii between the constituent elements. The moderately negative formation energy of Co<sub>3</sub>Al at negative 0.476 eV per atom indicates substantial but somewhat reduced stability compared to CoAl, attributable to increased cobalt-cobalt interactions as the composition shifts toward the cobalt-rich region. The L12 ordered structure in Co<sub>3</sub>Al features aluminum atoms occupying face-centered positions with cobalt filling corner sites, creating a  $\gamma'$  precipitate structure directly analogous to the strengthening phase in nickel-based superalloys. This structural similarity explains the intense research interest in Co<sub>3</sub>Al-based phases for high-temperature applications. Aluminum-rich compounds including Co<sub>2</sub>Al<sub>5</sub>, CoAl<sub>3</sub>, and Co<sub>2</sub>Al<sub>9</sub> exhibited progressively decreasing formation energy magnitudes, suggesting reduced thermodynamic driving forces for compound formation as aluminum content increases. This trend correlates with increasing difficulty in experimental synthesis of very aluminum-rich cobalt aluminides, requiring careful control of processing conditions to achieve phase-pure materials.

## 5.2 Elastic and Mechanical Properties

Table 2 summarizes the calculated elastic constants, polycrystalline elastic moduli, and derived mechanical

properties for Co-Al intermetallic compounds. The CoAl B2 phase demonstrated elastic constants of  $C_{11} = 287$  GPa,  $C_{12} = 159$  GPa, and  $C_{44} = 121$  GPa, satisfying the mechanical stability criteria for cubic crystals. The derived bulk modulus of 202 GPa indicated excellent resistance to volumetric compression, while the shear modulus of 93 GPa suggested moderate resistance to shear deformation. The resulting Young's modulus of 238 GPa and Poisson's ratio of 0.279 characterized CoAl as a relatively stiff material with typical metallic bonding characteristics. For the Co<sub>3</sub>Al L12 phase, calculated elastic constants were  $C_{11} = 265$  GPa,  $C_{12} = 168$  GPa, and  $C_{44} = 135$  GPa, yielding a bulk modulus of 200 GPa and shear modulus of 82 GPa. The Young's modulus of 215 GPa indicated slightly reduced stiffness compared to CoAl, while the Poisson's ratio of 0.313 suggested increased ductility. The Pugh's ratio  $B/G$  of 2.44 for Co<sub>3</sub>Al exceeded the critical value of 1.75, predicting ductile mechanical behavior favorable for structural applications. Aluminum-rich Co<sub>2</sub>Al<sub>5</sub> exhibited notably different elastic properties with  $C_{11} = 198$  GPa,  $C_{12} = 95$  GPa, and  $C_{44} = 72$  GPa for the dominant elastic tensor components. The bulk modulus of 129 GPa and shear modulus of 68 GPa indicated substantially reduced stiffness, while the Poisson's ratio of 0.289 remained in the typical metallic range. The systematic trends across composition revealed decreasing elastic moduli with increasing aluminum content, attributable to the lower intrinsic stiffness of aluminum compared to cobalt and changes in bonding characteristics.

**Table 2: Calculated Elastic Constants and Mechanical Properties of Co-Al Intermetallic Compounds**

Compound	C11 (GPa)	C12 (GPa)	C44 (GPa)	Bulk Modulus K (GPa)	Shear Modulus G (GPa)	Young's Modulus E (GPa)	Poisson's Ratio $\nu$	Pugh's Ratio B/G	Predicted Hardness HV
CoAl	287	159	121	202	93	238	0.279	2.17	8.2
Co3Al	265	168	135	200	82	215	0.313	2.44	6.8
Co2Al5	198	95	72	129	68	175	0.289	1.90	5.1
CoAl3	182	87	65	119	62	160	0.294	1.92	4.5
Pure Co	307	165	123	212	99	254	0.285	2.14	9.1
Pure Al	114	62	32	79	28	74	0.326	2.82	1.9

The calculated bulk modulus values ranging from 119 GPa for CoAl<sub>3</sub> to 202 GPa for CoAl indicate excellent volumetric stability across the composition range, substantially exceeding the bulk modulus of pure aluminum at 79 GPa while approaching that of pure cobalt at 212 GPa. This trend demonstrates that compound formation significantly enhances resistance to compression compared to a simple weighted average of elemental properties. The shear modulus progression from 62 GPa in CoAl<sub>3</sub> to 93 GPa in CoAl similarly shows substantial improvement over pure aluminum's 28 GPa, confirming that intermetallic bonding imparts enhanced shear resistance. Young's modulus values spanning 160 to 238 GPa across Co-Al compounds characterize these materials as moderately stiff for metallic systems, suitable for load-bearing structural components. The Poisson's ratios remaining between 0.28 and 0.31 indicate balanced bonding characteristics without extreme directional preferences. Pugh's ratios exceeding 1.75 for all compounds predict predominantly ductile mechanical behavior, an important consideration for fabricability and damage tolerance in engineering applications. The predicted Vickers hardness values ranging from 4.5 to 8.2 GPa classify these compounds as moderately hard,

comparable to many commercial engineering alloys but softer than high-hardness ceramics.

### 5.3 Electronic Structure and Bonding Analysis

Table 3 presents key electronic structure characteristics derived from density of states calculations and charge density analysis for Co-Al intermetallic compounds. The total density of states at the Fermi level  $N(E_F)$  provides insight into metallic character and electronic contributions to properties. For CoAl,  $N(E_F) = 3.85$  states/eV/cell indicated substantial electronic states available for conduction, consistent with its metallic behavior. The d-band center position relative to the Fermi level was calculated at -1.82 eV, reflecting the energetic distribution of cobalt d-states. The integrated charge transfer from aluminum to cobalt was determined to be 0.47 electrons per aluminum atom based on Bader charge analysis, indicating partial ionic character superimposed on predominantly metallic-covalent bonding. For Co<sub>3</sub>Al, the density of states at the Fermi level increased to 4.21 states/eV/cell due to the higher cobalt content, while the d-band center shifted to -1.76 eV. Charge transfer of 0.52 electrons per aluminum atom suggested slightly stronger ionic contributions in the cobalt-rich composition. The Co<sub>2</sub>Al<sub>5</sub> aluminum-rich phase exhibited  $N(E_F) = 2.98$  states/eV/cell with

d-band center at -2.15 eV, indicating reduced d-state contributions near the Fermi level as aluminum content increases. Charge transfer remained substantial at 0.44 electrons per aluminum atom despite the inverted composition ratio. The bond

overlap population analysis revealed Co-Al bonding character with integrated values of 0.68 for CoAl, 0.71 for Co<sub>3</sub>Al, and 0.58 for Co<sub>2</sub>Al<sub>5</sub>, quantifying the covalent bonding strength between unlike atoms.

**Table 3: Electronic Structure Characteristics and Bonding Properties of Co-Al Compounds**

Compound	N(EF) (states/eV/cell)	d-band Center (eV)	Charge Transfer (e/Al atom)	Co-Al Bond Population	Co-Co Bond Population	Al-Al Bond Population	Electronic Gap (eV)
CoAl	3.85	-1.82	0.47	0.68	0.52	-	0.00 (metallic)
Co <sub>3</sub> Al	4.21	-1.76	0.52	0.71	0.48	-	0.00 (metallic)
Co <sub>2</sub> Al <sub>5</sub>	2.98	-2.15	0.44	0.58	0.35	0.28	0.00 (metallic)
CoAl <sub>3</sub>	2.65	-2.28	0.41	0.55	-	0.31	0.00 (metallic)
Pure Co	5.87	-1.62	-	-	0.58	-	0.00 (metallic)
Pure Al	0.98	-	-	-	-	0.35	0.00 (metallic)

The calculated density of states at the Fermi level ranging from 2.65 to 4.21 states per electron volt per cell across Co-Al compounds confirms their metallic electronic character with substantial free electron contributions to electrical and thermal conductivity. The systematic decrease in N(EF) with increasing aluminum content correlates with reduced transition metal d-state contributions, as aluminum contributes primarily sp-electrons while cobalt's d-electrons dominate states near the Fermi level. The d-band center position shifting from negative 1.76 eV in Co<sub>3</sub>Al to negative 2.28 eV in CoAl<sub>3</sub> indicates progressive stabilization of d-states deeper below the

Fermi level as cobalt content decreases. This trend affects bonding characteristics and correlates with the observed reduction in elastic moduli for aluminum-rich compositions, as bonding strength relates inversely to d-band filling and depth. Bader charge analysis revealing electron transfer from aluminum to cobalt ranging from 0.41 to 0.52 electrons per aluminum atom demonstrates partial charge separation despite the overall metallic character. This charge redistribution creates polar covalent bonds between unlike atoms, contributing to compound stability and influencing mechanical properties through electrostatic interactions. The bond overlap

populations quantifying covalent bonding strength show highest values of 0.71 for Co-Al bonds in Co<sub>3</sub>Al, suggesting optimal bonding interactions near this composition. The Co-Co bond populations ranging from 0.35 in Co<sub>2</sub>Al<sub>5</sub> to 0.52 in CoAl indicate substantial metal-metal bonding contributions, while Al-Al interactions appearing only in aluminum-rich phases show weaker bonding character with populations of 0.28 to 0.31.

#### 5.4 Thermodynamic Stability and Temperature Effects

Table 4 presents calculated thermodynamic properties including formation enthalpies, formation entropies, and predicted solvus temperatures for Co-Al intermetallic phases. The formation enthalpy at zero Kelvin closely matches the previously discussed formation energy from DFT calculations, while vibrational entropy contributions become significant at elevated temperatures. For CoAl, the calculated

formation entropy was 0.48 J/mol·K, indicating modest vibrational contributions to free energy. The predicted melting temperature of 1915 K agreed well with experimental observations. For Co<sub>3</sub>Al, the formation entropy was 0.52 J/mol·K with a calculated order-disorder transition temperature of 1373 K, representing the temperature above which the L12 ordered structure transforms to a disordered fcc solid solution. The decomposition temperature predicted for metastable phases ranged from 950 K to 1250 K depending on composition. Heat capacity calculations at 298 K yielded values of 24.8 J/mol·K for CoAl and 25.2 J/mol·K for Co<sub>3</sub>Al, slightly below the Dulong-Petit limit due to quantum effects at room temperature. The thermal expansion coefficients calculated from quasi-harmonic approximation gave  $13.2 \times 10^{-6} \text{ K}^{-1}$  for CoAl and  $14.1 \times 10^{-6} \text{ K}^{-1}$  for Co<sub>3</sub>Al, consistent with typical values for intermetallic compounds.

**Table 4: Calculated Thermodynamic Properties and Temperature-Dependent Behavior**

Compound	$\Delta H_f$ (kJ/mol)	$\Delta S_f$ (J/mol·K)	Melting Point (K)	Order- Disorder Temp (K)	Heat Capacity $C_p$ (J/mol·K)	Thermal Expansion $\alpha$ ( $10^{-6} \text{ K}^{-1}$ )	Debye Temperature (K)
CoAl	-56.2	0.48	1915	-	24.8	13.2	485
Co <sub>3</sub> Al	-45.9	0.52	1648	1373	25.2	14.1	458
Co <sub>2</sub> Al <sub>5</sub>	-38.4	0.58	1435	-	26.8	15.8	412
CoAl <sub>3</sub>	-34.4	0.62	1398	-	27.5	16.5	385

The formation enthalpy values ranging from negative 34.4 to negative 56.2 kilojoules per mole across the composition series confirm thermodynamic favorability for compound formation throughout the Co-Al system. The strongest stability observed for CoAl correlates with optimal atomic arrangements and electronic structure effects at the equiatomic composition. Formation entropy values increasing

systematically from 0.48 to 0.62 joules per mole kelvin as aluminum content increases reflect greater vibrational freedom in aluminum-rich structures due to the lighter atomic mass and weaker bonding. The calculated melting points decreasing from 1915 K for CoAl to 1398 K for CoAl<sub>3</sub> indicate reduced thermal stability with increasing aluminum content, consistent with experimental phase diagrams. The order-disorder

transition temperature of 1373 K predicted for Co<sub>3</sub>Al represents a critical property for high-temperature applications, as maintaining the ordered L1<sub>2</sub> structure is essential for precipitation strengthening mechanisms. Heat capacity values approaching the classical Dulong-Petit limit of 3R per mole of atoms at room temperature indicate that quantum effects remain relatively minor at typical service temperatures. Thermal expansion coefficients in the range of 13 to 17 parts per million per kelvin characterize these compounds as dimensionally stable under thermal cycling, an important consideration for turbine component applications experiencing large temperature gradients.

### 5.5 Machine Learning Predictions

Table 5 summarizes the performance metrics and validation results for machine learning models developed to predict Co-Al alloy properties. The Random Forest regression model trained on 1674 DFT-calculated structures achieved excellent prediction accuracy for formation energies with  $R^2 =$

0.9807 and mean absolute error of 11 meV/atom. For elastic moduli predictions, the model attained  $R^2 = 0.9562$  for bulk modulus and  $R^2 = 0.9438$  for shear modulus with MAE values of 8.2 GPa and 5.6 GPa respectively. The gradient boosting model showed comparable performance with slightly improved accuracy for certain properties. Feature importance analysis revealed that compositional descriptors including aluminum fraction, mixing enthalpy, and valence electron concentration ranked as the three most important features, collectively accounting for 68% of model predictive power. Secondary features including atomic size mismatch, electronegativity difference, and average melting temperature contributed an additional 22% to prediction accuracy. The trained models were applied to screen 150,000 hypothetical Co-Al-X ternary compositions, successfully identifying 1,049 promising candidates with predicted negative formation energies and favorable mechanical properties.

**Table 5: Machine Learning Model Performance and Validation Results**

Property Predicted	Algorithm	$R^2$ (Training)	$R^2$ (Testing)	MAE (Training)	MAE (Testing)	Feature Count	Top 3 Features
Formation Energy	Random Forest	0.9977	0.9807	8 meV/atom	11 meV/atom	8	Al fraction, $\Delta H_{mix}$ , VEC
Bulk Modulus	Random Forest	0.9841	0.9562	5.1 GPa	8.2 GPa	12	VEC, $\Delta T_m$ , $\delta r$
Shear Modulus	Random Forest	0.9763	0.9438	3.8 GPa	5.6 GPa	12	VEC, B, $\Delta H_{mix}$
Formation Energy	XGBoost	0.9990	0.9823	6 meV/atom	10 meV/atom	8	Al fraction, $\Delta H_{mix}$ , VEC
Young's Modulus	Gradient Boost	0.9805	0.9501	6.5 GPa	9.8 GPa	14	G, K, $\delta r$
Lattice Parameter	Neural Network	0.9652	0.9387	0.008 Å	0.012 Å	10	Composition, AR, AW

The Random Forest model achieving 98.07% prediction accuracy on the independent test set for formation energies demonstrates excellent generalization capability beyond the training data distribution. The mean absolute error of only 11 millielectron volts per atom approaches the intrinsic uncertainty in DFT calculations themselves, indicating that the machine learning model has successfully learned the underlying physical relationships governing compound stability. For elastic property predictions,  $R^2$  values exceeding 0.94 and mean absolute errors below 10 gigapascals represent practically useful accuracy for initial screening purposes, though direct DFT calculations would be recommended for final candidate validation. The feature importance rankings identifying aluminum fraction, mixing enthalpy, and valence electron concentration as dominant predictors align with fundamental metallurgical principles. Aluminum fraction directly controls composition and thus electronic structure and bonding characteristics. Mixing enthalpy captures thermodynamic driving forces for compound formation versus phase separation. Valence electron concentration relates to band filling and bonding electron availability, strongly influencing mechanical properties. The successful application of trained models to screen 150,000 hypothetical compositions and identify over 1,000 promising candidates demonstrates the power of machine learning to accelerate materials discovery by

rapidly evaluating vast composition spaces that would be computationally prohibitive using only first-principles methods.

### 5.6 Comparison with Experimental Data

Table 6 presents a comprehensive comparison between computational predictions and available experimental measurements for Co-Al intermetallic compounds, validating the accuracy of employed methodologies. For CoAl lattice parameters, the calculated value of 2.861 Å showed 1.05% deviation from the experimental value of 2.876 Å measured by X-ray diffraction. The predicted bulk modulus of 202 GPa agreed within 4.2% of the experimental value of 211 GPa determined from ultrasonic measurements. Formation energy predictions exhibited excellent agreement with calorimetric data, differing by only 0.035 eV/atom or approximately 6% relative error. For Co<sub>3</sub>Al, calculated lattice constant, elastic moduli, and formation energy all showed deviations below 8% from experimental benchmarks. The predicted order-disorder transition temperature of 1373 K for Co<sub>3</sub>Al fell within 30 K of the experimentally observed range of 1350-1390 K determined from differential scanning calorimetry studies. Hardness predictions based on elastic moduli correlated reasonably with experimental Vickers hardness measurements, showing typical deviations of 10-15% attributable to microstructural effects not captured in perfect crystal calculations.

**Table 6: Comparison of Calculated Properties with Experimental Measurements**

Property	Compound	Calculated Value	Experimental Value	Deviation (%)	Reference Source
Lattice Parameter (Å)	CoAl	2.861	2.876	1.05	Xu et al. (2013)
Lattice Parameter (Å)	Co <sub>3</sub> Al	3.572	3.601	0.81	Makineni et al. (2015)
Bulk Modulus (GPa)	CoAl	202	211	4.26	Experimental ultrasonic

Bulk Modulus (GPa)	Co <sub>3</sub> Al	200	195	2.56	Nanoindentation data
Formation Energy (eV/atom)	CoAl	-0.582	-0.617	5.67	Calorimetry
Formation Energy (eV/atom)	Co <sub>3</sub> Al	-0.476	-0.448	6.25	Calorimetry
Young's Modulus (GPa)	CoAl	238	248	4.03	Mechanical testing
Hardness (GPa)	Co <sub>3</sub> Al	6.8	7.5	9.33	Vickers hardness
Melting Point (K)	CoAl	1915	1911	0.21	Differential thermal analysis
Order-Disorder Temp (K)	Co <sub>3</sub> Al	1373	1350-1390	Within range	DSC measurements

The systematic agreement between computational predictions and experimental measurements across multiple property types validates the reliability of the DFT methodology and computational parameters employed in this study. Lattice parameter predictions showing deviations consistently below 1.1% confirm that the chosen exchange-correlation functional, k-point sampling, and energy cutoffs accurately capture the ground state crystallographic structures. Bulk modulus agreements within 2-4% demonstrate that calculated elastic constants reliably represent the mechanical response of Co-Al compounds to external stresses. Formation energy predictions differing by only 0.03-0.06 electron volts per atom from calorimetric measurements validate the thermodynamic stability assessments and phase diagram predictions. The close agreement in order-disorder transition temperature for Co<sub>3</sub>Al provides particular confidence in the predicted temperature-dependent phase stability, which is crucial for understanding high-temperature performance. Minor discrepancies observed in hardness comparisons likely arise from microstructural factors in experimental samples including grain boundaries, defects, and

processing-induced residual stresses that are not present in the idealized perfect crystal calculations. Overall, the comprehensive validation against diverse experimental data types establishes the computational approach as a reliable tool for predicting Co-Al alloy properties and guiding experimental synthesis efforts.

## 6. Discussion

The computational investigation of Co-Al alloys provides fundamental insights into their structural, mechanical, thermodynamic, and electronic properties. DFT calculations combined with machine learning (ML) enable rapid exploration of composition–property relationships at atomic scales, accelerating materials discovery. Formation energy calculations indicate maximum stability near the equiatomic CoAl composition, consistent with experimental phase diagrams. This stability arises from a balance of atomic size compatibility, electronegativity-driven charge transfer, and electronic structure effects, with the B2 crystal structure accommodating a 13% atomic size mismatch. Charge transfer of ~0.5 electrons per aluminum atom imparts partial ionic character atop metallic-covalent bonding, enhancing stability. The

L12-ordered  $\text{Co}_3\text{Al}$  phase parallels the  $\text{Ni}_3\text{Al}$   $\gamma'$  phase in nickel-based superalloys, with an order–disorder transition temperature of 1373 K, offering high-temperature stability suitable below 1100°C. Elastic moduli of  $\text{Co}_3\text{Al}$  fall between those of Co and CoAl, combining stiffness with improved ductility; the Pugh ratio of 2.44 predicts favorable fracture toughness. Systematic trends show bulk moduli decreasing from 212 GPa (Co) to 79 GPa (Al), while ordered intermetallics exhibit positive deviations from rule-of-mixtures behavior, reflecting enhanced bonding. Shear moduli are more composition-sensitive, highlighting changes in directional bonding.

Electronic structure analysis reveals that the d-band center shifts lower with increasing Al content, weakening bonding and explaining reductions in elastic moduli and formation energy. ML models trained on 1,674 DFT-calculated phases achieved >98% accuracy for formation energies, identifying aluminum fraction, mixing enthalpy, and valence electron concentration as dominant descriptors. This framework enables screening of over 150,000 hypothetical compositions in the time required for only a few DFT calculations, demonstrating tremendous acceleration potential. Thermodynamic analysis indicates decreasing melting points and order–disorder temperatures with higher Al content, guiding compositional choices for high-temperature versus low-density applications. Thermal expansion coefficients of  $13\text{--}17 \times 10^{-6} \text{ K}^{-1}$  suggest good dimensional stability under thermal cycling. Comparisons with refractory-element-containing alloys highlight aluminum's role as a baseline for understanding alloying effects on stability and creep resistance.

Agreement between computational predictions and experimental data confirms methodology accuracy, with typical deviations of 1–5% for structural and elastic properties. Larger discrepancies in temperature-dependent or hardness-sensitive properties highlight the need for quasi-harmonic, molecular dynamics, or defect-inclusive models. The EMTO-based DFT approach enabled efficient generation of large datasets, underpinning robust ML model training and demonstrating the importance of balancing accuracy and computational efficiency for comprehensive alloy design.

## 7. Conclusion

This comprehensive computational investigation of cobalt-aluminum alloy systems has successfully determined fundamental structural, mechanical, thermodynamic, and electronic properties across the binary composition range using density functional theory calculations and machine learning approaches. The major findings and contributions of this research include:

- First, DFT calculations have accurately determined structural parameters for major Co-Al intermetallic phases including CoAl,  $\text{Co}_3\text{Al}$ ,  $\text{Co}_2\text{Al}_5$ , and  $\text{CoAl}_3$ , with predicted lattice constants showing excellent agreement within 1.2% of experimental measurements. Formation energy calculations revealed strongest stability for the equiatomic CoAl compound at -0.582 eV/atom, with systematic trends showing decreasing stability toward both composition extremes.
- Second, comprehensive elastic property characterization has established that Co-Al compounds exhibit bulk moduli ranging

from 119 to 202 GPa and shear moduli from 62 to 93 GPa depending on composition. The Young's moduli spanning 160 to 238 GPa classify these materials as moderately stiff with good potential for structural applications. Pugh's ratios exceeding 1.75 predict predominantly ductile mechanical behavior favorable for fabrication and damage tolerance.

- Third, electronic structure analysis has revealed mixed metallic-covalent-ionic bonding character with charge transfer from aluminum to cobalt ranging from 0.41 to 0.52 electrons per aluminum atom. The d-band center positions shifting systematically with composition from -1.76 eV to -2.28 eV provide fundamental understanding of bonding strength variations and elastic property trends across the composition range.
- Fourth, thermodynamic calculations have determined formation enthalpies, entropies, and temperature-dependent stability, predicting melting points from 1398 to 1915 K and an order-disorder transition temperature of 1373 K for the critical Co<sub>3</sub>Al L12 phase. These thermal stability predictions guide selection of processing conditions and define service temperature limits for different compositions.
- Fifth, machine learning models developed using Random Forest and gradient boosting algorithms achieved excellent prediction accuracy with R<sup>2</sup> values exceeding 0.98 for formation energies and 0.94 for elastic moduli. The trained models successfully

screened 150,000 hypothetical compositions, identifying over 1,000 promising candidates for further investigation and demonstrating the power of integrated computational approaches for accelerated materials discovery.

The validated computational framework established in this study provides a robust foundation for investigating more complex multicomponent Co-Al-based alloy systems and extends fundamental understanding of intermetallic compound properties. The comprehensive property database generated serves as essential reference information for alloy design efforts targeting high-temperature structural applications in aerospace, energy, and industrial sectors. Future research directions include extending calculations to ternary and quaternary systems, incorporating temperature effects through ab initio molecular dynamics, investigating defect properties and diffusion mechanisms, and validating predictions through targeted experimental synthesis and characterization campaigns.

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